

3.2

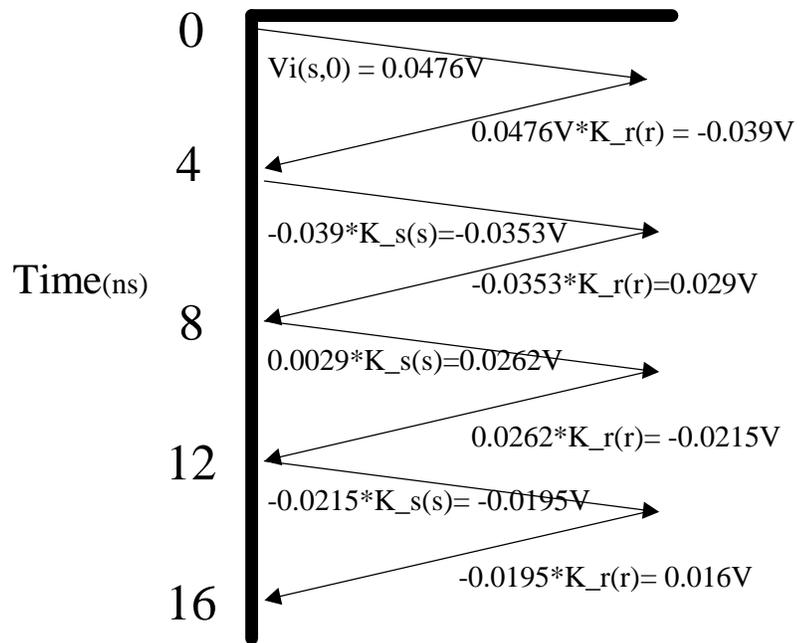
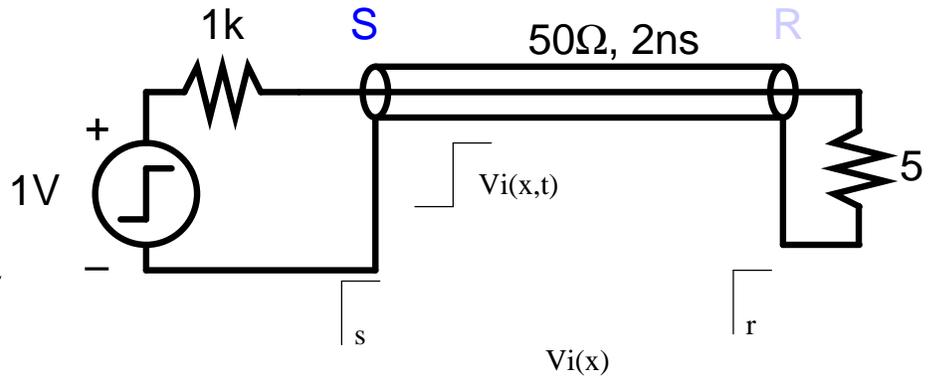
$$K_{r(r)} = \left[\begin{matrix} _r \\ _r \end{matrix} \right] = \frac{5-50}{5+50} = -0.82$$

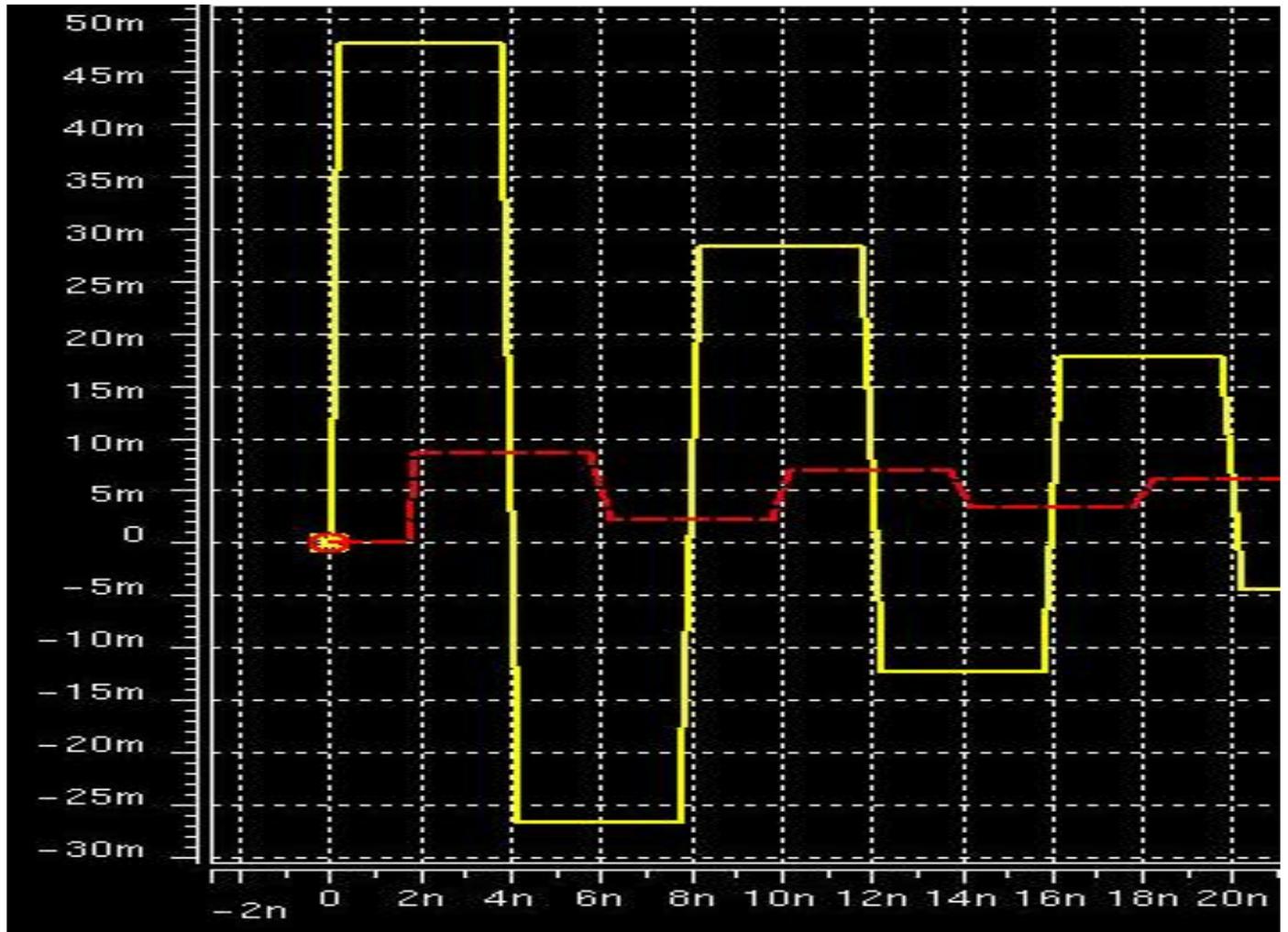
$$K_{s(s)} = \left[\begin{matrix} _s \\ _s \end{matrix} \right] = \frac{1k-50}{50+1k} = 0.905$$

Initial pulse(to transmission line) =

$$Vi(s,0) = 1V * \frac{50}{1k+50} = 0.0476V$$

Time(ns)	V(s,t)	V(r,t)
0	0.0476	0
2	0.0476	0.0086
4	-0.0267	0.0086
6	-0.0267	0.0023
8	0.0285	0.0023
10	0.0285	0.007
12	-0.0125	0.007
14	-0.0125	0.0035
16	0.018	0.0035



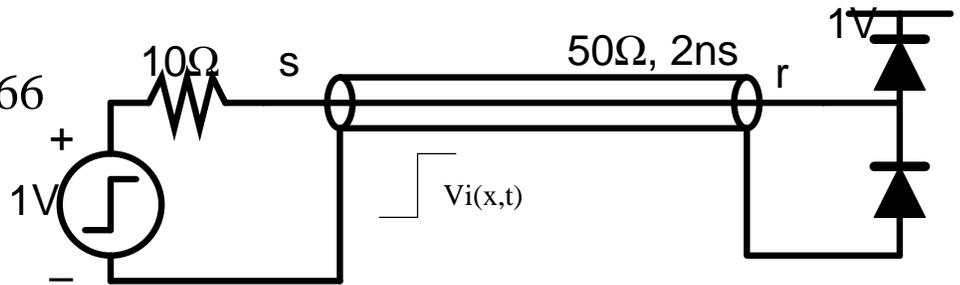


3.10

$$K_{r(r)} = \Gamma_r = \frac{10-50}{50+10} = -0.66$$

Initial pulse(to transmission line) =

$$V_i(s,0) = 1V * \frac{50}{10+50} = 0.833V$$

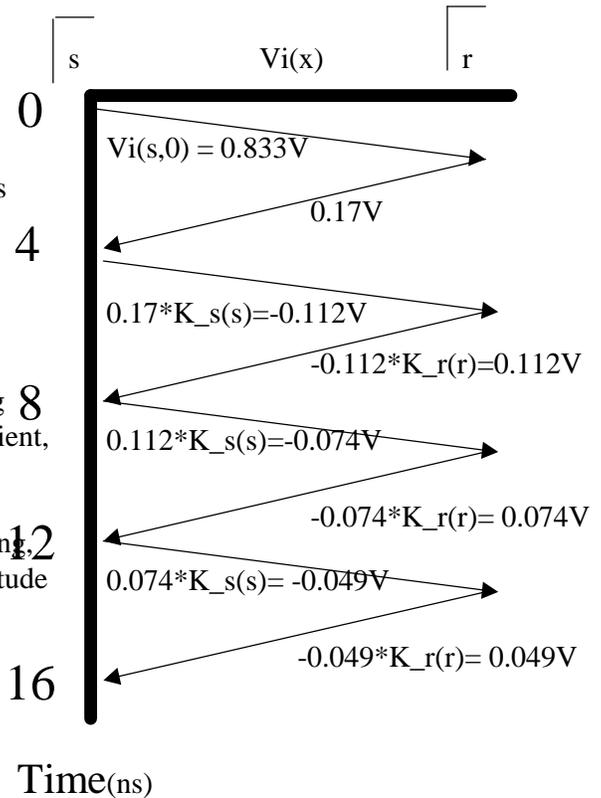


At the beginning of time, $V(r)=0V$. Assume that both diodes are not conducting. In this case, $V(r)$ looks like an open circuit.

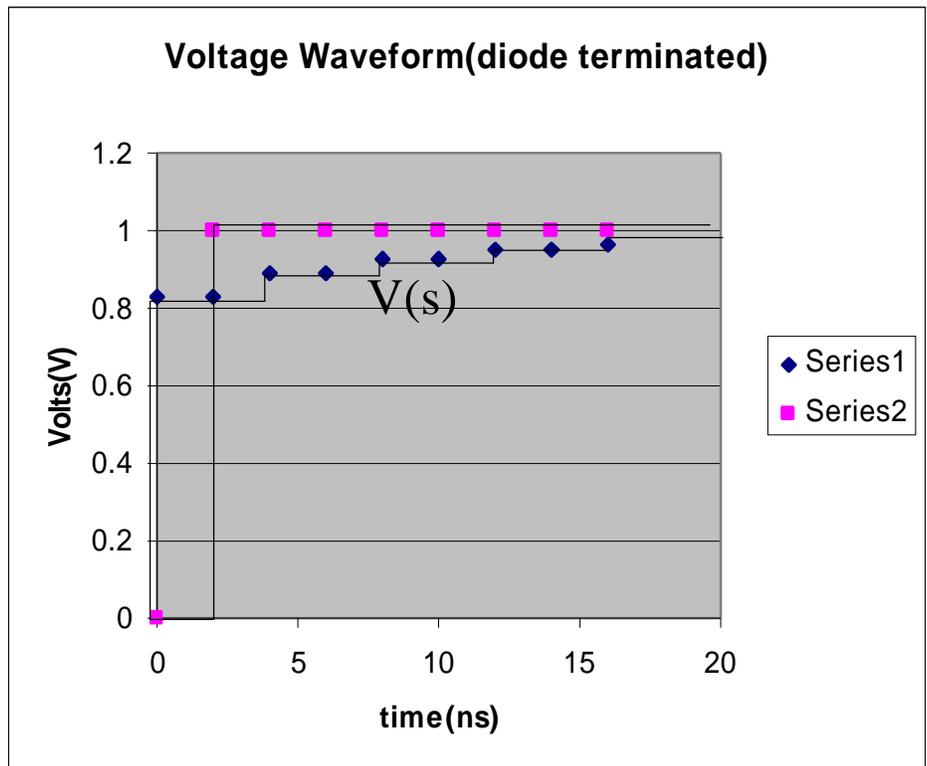
A wave of 0.83V hits the end of the line. Nominally, for an open circuit, the wave will get reflected back with $K_{r(r)}=1$. That means that $V(r)=1.66V$. However, we know that once $V(r)=1V$, the top diode becomes conducting, forcing $V(r)=1V$. Therefore, it is impossible for 0.83V to reflect back.

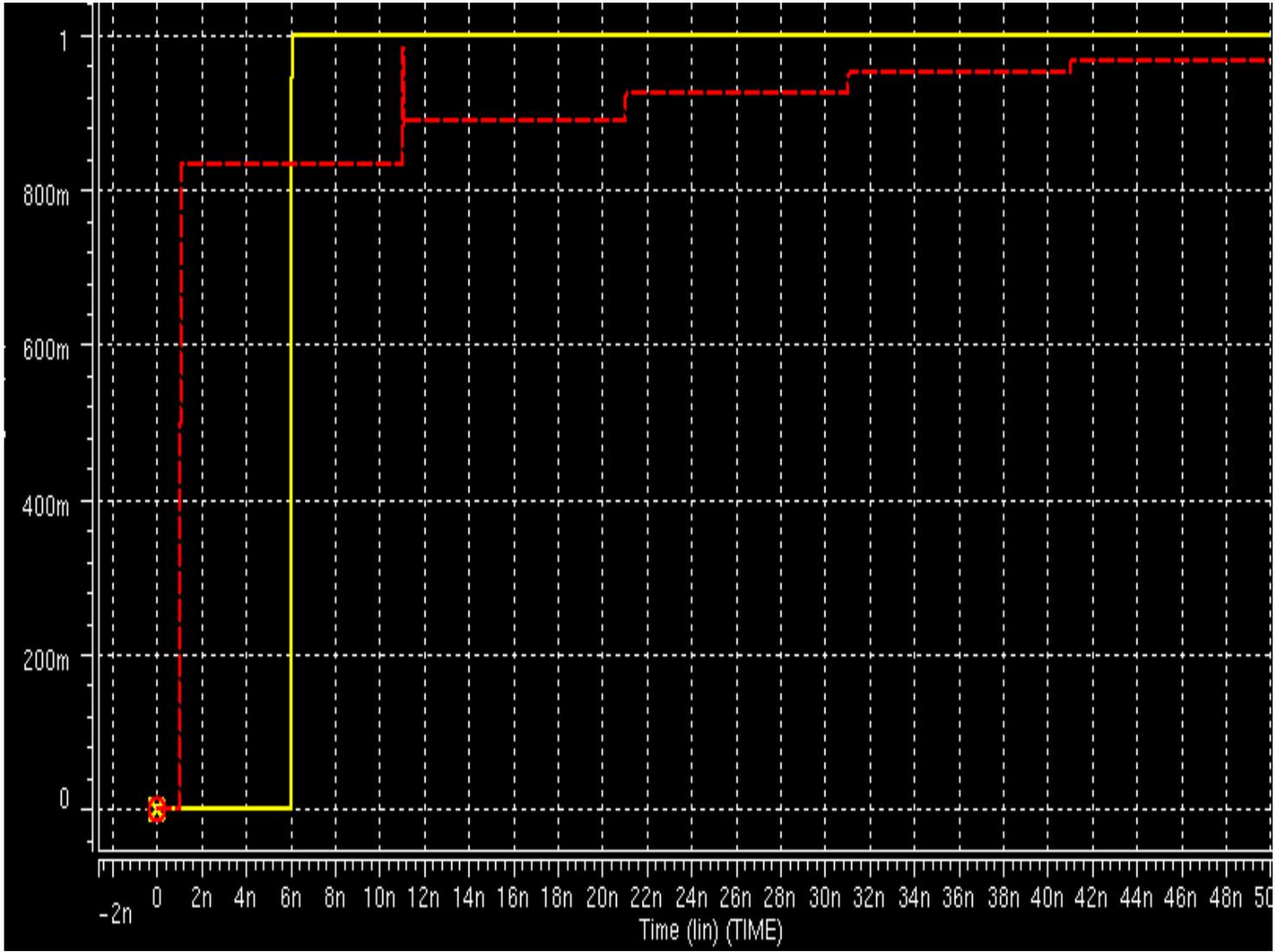
Instead, a wave of $1-0.83V=0.17V$ is reflected backwards to $V(s)$, in order for $V(r)=0.83V+0.17V=1V$. This 0.17V is now a traveling wave back to the source, where it sees a negative reflection coefficient, so that a $-0.66*0.17=-0.112V$ wave now is heading towards $V(r)$.

However, when this wave hits $V(r)$, since the top diode is conducting, $K_{r(r)}=-1$. So this -0.112V gets reflected back as a wave of magnitude 0.112V. This basically “rings” up the source voltage, while $V(r)$ rings up with the initial step voltage.



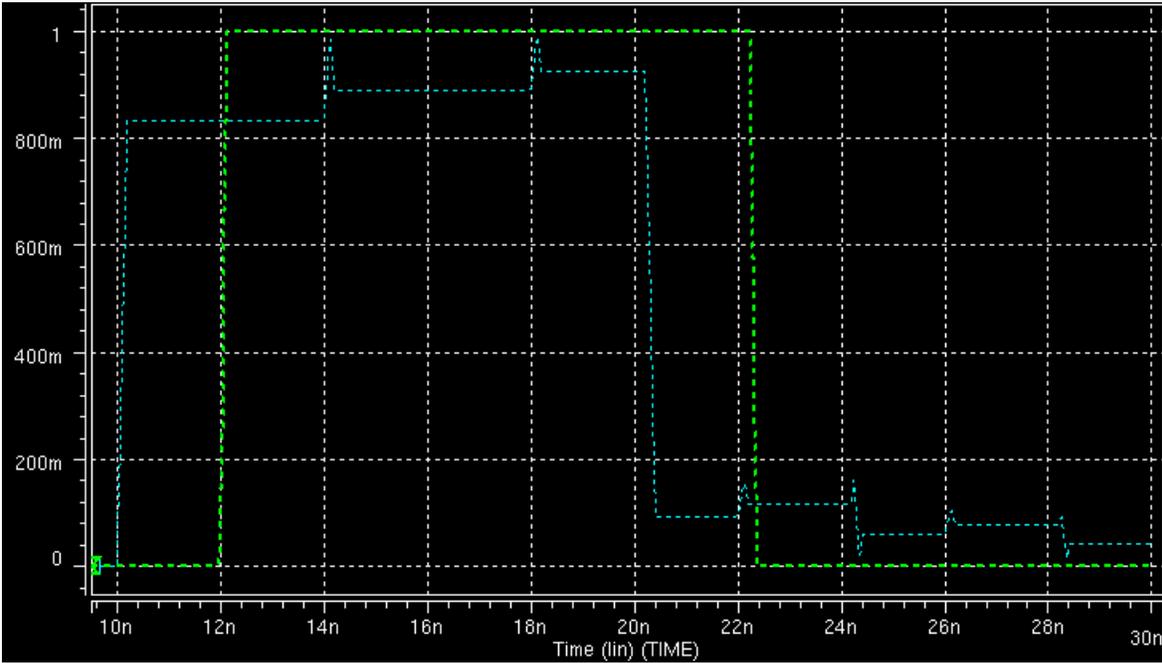
Time(ns)	Source(Vs)	Termination(Vr)
0	0.83	0
2	0.83	1
4	0.888	1
6	0.888	1
8	0.926	1
10	0.926	1
12	0.951	1
14	0.951	1
16	0.966	1





You can also consider the reflection process with currents as opposed to voltages ringing along the line. The initial pulse puts a current of $1V/60 = 16.6mA$ into the line. At the far end, which is terminated by the diodes, $3.4mA$ reflects back and $13.2mA$ goes into the diode. When the $3.4mA$ reaches the source, $-2.2mA$ reflects back. When this gets to the far end, it reduces the $13.2mA$ to $11.0mA$, but since this is greater than 0 the diode remains conducting and a negative reflection occurs -- reducing the diode current to $8.8mA$. And so on.

The following spice waveform shows what happens when the diode connected system is input with a much slower input step edge. ($200ps$ vs $10ps$) Since the input voltage doesn't rise to $1V$ fast enough, the input into the line will not be an immediate $0.83V$, but instead, a slower rise to $0.83V$. This means that the reflection at the end of the line will see an open circuit for longer time, since the pulse doesn't rise to $0.83V$ that fast. In this manner, you see the reflected pulses from the transmitter termination go to $1V$ and then settle back to the values that were calculated above, due to the finite time of the input rise time.



Input waveform for a slow input rise time (200ps)